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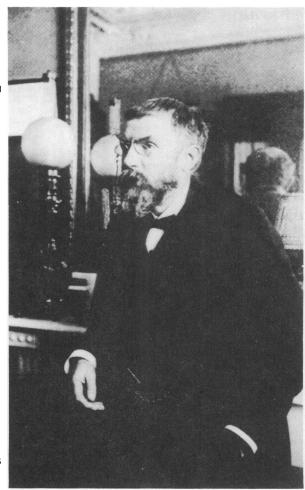
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- §3. Riemann surfaces, discontinuous groups and Lie groups Lipman Bers Wilfried Schmid Dennis Sullivan
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Each column in the first portion of this chapter contains classification codes from the 1980 system, codes used in the cumulative index covering 1973 to 1979, verbal headings, and corresponding Library of Congress classification numbers.

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## World Directory of Mathematicians 1982

The seventh edition of this directory, which is based on material supplied by the National Committees for Mathematics, is published by the Bureau of the World Directory of Mathematicians of the International Mathematical Union. Some of the national committees failed to offer new entries; in these cases the entries from the sixth edition have been used. The seventh edition contains a list of important mathematical organizations, an alphabetical list of mathematicians with addresses, and a geographical list. The AMS is distributing the directory.

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## Singularities Peter Orlik, Editor PROCEEDINGS OF SYMPOSIA IN PURE MATHEMATICS, VOLUME 40

This book presents the proceedings of the Summer Institute on Singularities held at Humboldt State University, Arcata, California on July 20-August 7, 1981, and was prepared with partial support from the National Science Foundation.

The Theory of Singularities is a relatively new area of research which has grown rapidly and developed into a major field of activity. It employs the tools of Algebraic Geometry, Algebraic Topology, Differential Geometry and Real and Complex Analysis. The basic aim of these volumes is to give an exposition of the area, describe recent progress and list open problems. Some of the major topics are resolution and deformation of singularities in the algebraic and analytic categories; smoothing theory and mixed Hodge structures; equisingularity, the study of polar varieties and Whitney stratifications; Milnor fibration, monodromy and intersection pairing; analytic results, including the Gauss-Manin connection and relations with differential systems; metric properties and curvature; connections with knot theory and link theory, equivariant results and automorphic forms; unfoldings, adjacency, classification of singularities and modality; stability of singularities; Newton diagrams; Morse theory and intersection homology; and applications to physics and other sciences.

The expository papers introduce the reader to the frontiers of broad areas of research activity in singularities. The research articles solve specific problems and pose related open questions. In addition, two articles are devoted entirely to open problems in the area. Background necessary for understanding the papers is two years of graduate-level mathematics with advanced courses in Algebraic Topology, Algebraic Geometry, and Analysis.

The book's most significant contribution is its breadth. It encompasses the entire spectrum of research in singularities at this time. The field is very active and this is the first attempt at such comprehensive coverage.

Following is a list of contributors:

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# PROCEEDINGS OF SYMPOSIA IN PURE MATHEMATICS

## Operator Algebras and Applications Richard V. Kadison, Editor

These volumes present a state-of-the-art account of the theory of operator algebras and its applications. They stem from a conference that represented the first meeting dealing with the full range of the subject in over thirteen years. The major part of the volumes is expository in nature—the conference was arranged to survey advances and developments in recent years. Many articles have been written to give expository descriptions of these advances. There are groups of related articles (for example, in the theory of  $C^*$ -dynamical systems, the theory of unbounded derivations, applications to quantum physics, and the cohomology theory of operator algebras). There are major articles by many of the leading contributors to the field.

The Symposium was held at Queen's University, Kingston, Ontario, July 14–August 2, 1980. It was partially supported by a grant from the National Science Foundation.

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# AMS SHORT COURSE LECTURE NOTES A Subseries in Proceedings of Symposia in Applied Mathematics (ISSN 0160-7634)

## Statistical Data Analysis Ram Gnanadesikan, Editor

This book is an outcome of the 1982 AMS Short Course given at Toronto. Statistical data analysis has been receiving a great deal of attention recently as evidenced by the fact that subsets of the authors of the present volume have given workshops or short courses on this topic at various meetings in the last two years, including those of the Mathematical Association of America and ICME-IV. The interest may be due to many things—practical importance of the topic, challenging research problems in a relatively young field, need for ideas and material for teaching courses on the subject.

Clearly neither the short course nor this book can provide enough details on all of the above facets of interest. However, the different chapters do address these aspects, although with varying degrees of emphasis. One hope of all the authors in publishing this book is that others will use this material as a starting point and, with the help of some of the references, be able to develop workshops, short courses and other educational forums on their own.

The authors are all employed by Bell Laboratories which provided support for the efforts of all of them.

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- R. Gnanadesikan, Introduction
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# Homology and Dynamical Systems John M. Franks

This book is an exposition of a number of results dealing with the connections between algebraic topology and dynamical systems. For the most part proofs are included; where they are omitted a reference is given. The topics covered include: Morse gradients, symbolic dynamics and subshifts of finite type, Smale and Morse-Smale diffeomorphisms and flows, and the zeta function and homology zeta function of a diffeomorphism.

The book is intended for graduate students or researchers interested in the relationship between topology and dynamical systems. It is especially appropriate for persons with a background in topology who want to learn about dynamical systems. This book would be appropriate for a graduate level course. Except for an assumed background in algebraic topology the material is largely self-contained.

There are numerous books on algebraic topology and many on dynamical systems. This is the only book devoted to the inter-relationships of these two fields.

1980 Mathematics Subject Classifications: 58F09; 57R50 CBMS Regional Conference Series Number 49, vii + 120 pages (soft cover) List price \$14, individuals \$7 ISBN 0-8218-1700-0; LC 82-8897 Publication date: September 1982 To order, please specify CBMS/49K

# Selected Topics in Harmonic Maps James Eells and Luc Lemaire

The first part of this work is devoted to an account of various aspects of the theory of harmonic maps between Riemannian manifolds. In §1 the authors develop the formalism of Riemannian connections in vector bundles and the relevant calculus of vector bundle valued differential forms. That formalism is applied systematically in the sequel.  $\S$  2–7 give a rather full treatment of various topics.  $\S$  8 and 9 present certain aspects of the relationships between harmonic and holomorphic maps.

The primary aim of Part I is to present a coherent introduction to harmonic maps as a branch of geometric variational theory, and to illustrate their appearance as significant objects in Riemannian geometry.

In Part II the authors propose certain unsolved problems, together with comments and references. They range over the whole theory of harmonic maps, and are certainly of widely varying difficulty.

This book presents the first printed exposition of the qualitative aspects of harmonic maps.

#### Contents

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- §§1. Operators on vector bundles, 2. Harmonic maps, 3. Some properties of harmonic maps, 4. Second variation of the energy, 5. Spheres and the behavior of the energy, 6. The stress-energy tensor, 7. Harmonic morphisms, 8. Holomorphic and harmonic maps between almost Kähler manifolds, 9. Properties of harmonic maps between Kähler manifolds.
- Part II. Problems Relating to Harmonic Maps §§1. Existence of harmonic maps, 2. Regularity problems, 3. Holomorphic and conformal maps, 4. Construction/classification of harmonic maps, 5. Properties of harmonic maps, 6. Spaces of maps, 7. Noncompact domains, 8. Variations on a theme.

1980 Mathematics Subject Classifications: 58E20; 32H99, 49F99, 53C05, 58A10, others.

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